

## 14-4, 14-5 Multiplying Polynomials

**\*Remember:**

1. When we are multiplying integers, variables, or other terms, if they have

Different signs  $\rightarrow$  answer is negative      Same signs  $\rightarrow$  answer is positive

$$9 * -2 = \underline{-18}$$

$$-9 * -2 = \underline{18}$$

2. When we multiply terms with exponents, we add the exponents of the like terms. (must have the same base)

$$a^5 * a^4 = \underline{a^9}$$
  
$$5+4=9$$

$$b^7 * b^2 = \underline{b^5}$$
  
$$7+(-2)$$

$$\text{Ex: } \underline{x^2} * \underline{x^3}$$

Ex. 1: Multiply using Distributive Property. Then, simplify if needed.

A.  $(9x^5y^7)(-2x^4y^4)$

$$(9 \cdot -2)(x^5 \cdot x^4)(y^7 \cdot y^4)$$
  
$$\boxed{-18x^9y^{11}}$$

- ① Multiply coefficients
- ② Multiply 1<sup>st</sup> variable
- ③ Multiply 2<sup>nd</sup> variable

B.  $(-4x^3y^2)(-7x^5y^3)$

$$(-4 \cdot -7)(x^3 \cdot x^5)(y^2 \cdot y^3)$$
  
$$\boxed{28x^8y^5}$$

C.  $3(5x + 2y^2)$  \*use distributive property

$$3 \cdot 5x + 3 \cdot 2y^2$$

$$\boxed{15x + 6y^2}$$

D.  $8y(5x^2 - 2y)$

$$8y \cdot 5x^2 - 8y \cdot 2y$$
  
$$\boxed{40x^2y - 16y^2}$$

Note:

- 1) List variables in alphabetical order
- 2) Greatest exponents first

E.  $-7x^9y^4(6x^3y + x^2 - 4xy^5 - 8)$

$$(-7x^9y^4 \cdot 6x^3y) + (-7x^9y^4 \cdot x^2) + (-7x^9y^4 \cdot -4xy^5) + (-7x^9y^4 \cdot -8)$$
  
$$\boxed{42x^{12}y^5 - 7x^{10}y^4 + 28x^{10}y^9 + 56x^9y^4}$$

F.  $-4x^2y^3(-5xy^4 + 3x^4) - x^3y^7 + 8$  \*combine like terms

$$20x^3y^7 - 12x^6y^3 - x^3y^7 + 8$$
  
$$\boxed{19x^3y^7 - 12x^6y^3 + 8}$$

When multiplying a binomial by a binomial, we still use the distributive property. However, we have a method that helps us keep our work organized called the

FOIL method.F  $\rightarrow$  firstO  $\rightarrow$  outerI  $\rightarrow$  innerL  $\rightarrow$  last

$$(x + 4)(x - 1)$$

$$(x)(x) + (x)(-1) + (4)(x) + (4)(-1)$$

$$x^2 - x + 4x - 4$$
  
$$\boxed{x^2 + 3x - 4}$$

Ex. 2: Multiply using the foil method.

A.  $(x + 3)(x + 2)$

$$(x)(x) + (x)(2) + (3)(x) + (3)(2)$$

$$x^2 + \underline{2x} + \underline{3x} + \underline{6}$$

$$\boxed{x^2 + 5x + 6}$$

C.  $(7m + 2)(3m - 8)$

$$21m^2 - 56m + 6m - 16$$

$$\boxed{21m^2 - 50m - 16}$$

E.  $(a - 2)(b - 8)$

$$ab - 8a - 2b + 16$$

B.  $(2y + 1)(5y + 3)$

$$10y^2 + 6y + 5y + 3$$

$$\boxed{10y^2 + 11y + 3}$$

D.  $(3c - 5a)(2c + 4d)$

$$6c^2 + 12cd - 10ac - 20ad$$

### Special Products:

$$1. (a+b)^2 = (a+b)(a+b)$$

$$a^2 + ab + ab + b^2$$

$$\boxed{a^2 + 2ab + b^2}$$

↑      PERFECT SQUARE TRINOMIALS      ↑

$$2. (a-b)^2 = (a-b)(a-b)$$

$$a^2 - ab - ab + b^2$$

$$\boxed{a^2 - 2ab + b^2}$$

$$3. (a+b)(a-b)$$

$$a^2 - \underbrace{ab + ab}_{\text{zero pair}} - b^2$$

$$\boxed{a^2 - b^2}$$

DIFFERENCE OF TWO SQUARES

Ex. 3: Multiply using the foil method and the trick using the pattern with the special products.

A.  $(x+3)^2$

$$(x+3)(x+3)$$

$$x^2 + 3x + 3x + 9$$

$$\boxed{x^2 + 6x + 9}$$

B.  $(y-4)^2$

$$(y-4)(y-4)$$

$$y^2 - 4y - 4y + 16$$

$$\boxed{y^2 - 8y + 16}$$

C.  $(x+7)(x-7)$

$$x^2 - 7x + 7x - 49$$

$$\boxed{x^2 - 49}$$

\* Compare with :

$$(x-3)^2$$



$$\boxed{x^2 - 6x + 9}$$

$$(y-4)^2$$



$$\boxed{y^2 - 8y + 16}$$

$$(x+7)(x-7)$$

$$\boxed{x^2 - 49}$$

1<sup>st</sup> term squared

2 x 1<sup>st</sup> term x 2<sup>nd</sup> term

2<sup>nd</sup> term squared

} Perfect Square  
Trinomials

Difference  
of Two Squares

} 1<sup>st</sup> term squared  
minus  
2<sup>nd</sup> term squared