

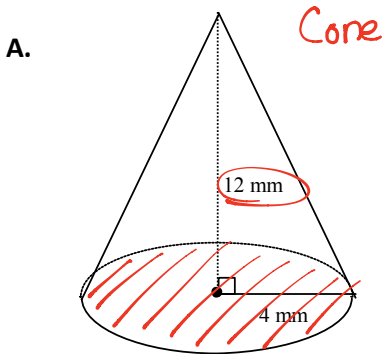
10-1F Volume Notes: Cones

Volume – the space that a three-dimensional figure occupies *units cubed

For **Cones** – circular base across from apex

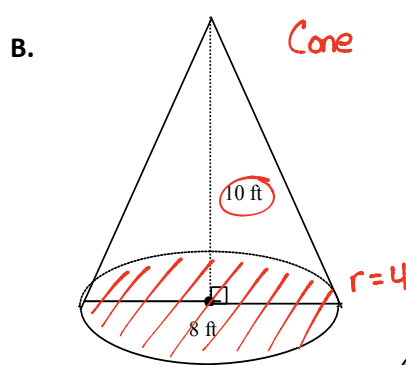
$$V = \frac{Bh}{3} \quad V = \frac{1}{3}Bh$$

Ex. 1: Find the volume of each cone. Round to the nearest tenth if necessary.



$$\begin{aligned} V &= \frac{Bh}{3} \\ &= \frac{(\pi r^2)h}{3} \quad \text{area of circle} \\ &= \frac{\pi(4)^2(12)}{3} \\ &= \frac{3.14(16)(12)}{3} \end{aligned}$$

$$V = 201 \text{ mm}^3$$



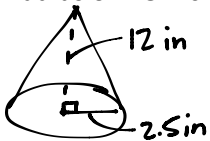
$$\begin{aligned} V &= \frac{\pi r^2 h}{3} \\ &= \frac{\pi(4)^2(10)}{3} \\ &= \frac{3.14(16)(10)}{3} \end{aligned}$$

$$V = 167.5 \text{ ft}^3$$

KEY TIPS:

- 1) Circle (height of figure)
- 2) Shade (bases)
- 3) Name (figure using the shape of the base)
- 4) Write basic formula for 3-D figure
- 5) Write specific formula (according to base)
- 6) Substitute values
- 7) Calculate
- 8) Check units/rounding

Ex. 2: Find the volume of a cone that has a height of 12 inches and a radius of 2.5 inches.



$$\begin{aligned} V &= \frac{\pi r^2 h}{3} \\ &= \frac{\pi(2.5)^2(12)}{3} \\ &= \frac{3.14(6.25)(12)}{3} \end{aligned}$$

$$V = 78.5 \text{ in}^3$$

Ex. 3: A cone with a diameter of 4 feet has a volume of 29.3 cubic feet. Find the height of the cone.

$$\begin{aligned} V &= 29.3 \text{ ft}^3 \\ d &= 4 \text{ ft} \rightarrow r = 2 \text{ ft} \\ h &= ? \end{aligned}$$

$$\begin{aligned} V &= \frac{\pi r^2 h}{3} & 29.3 &= \frac{3.14(2)^2 h}{3} \\ 29.3 &= \frac{3.14(4)h}{3} \\ 29.3 &= \frac{4.2h}{4.2} \end{aligned}$$

$$h = 7 \text{ ft}$$

Ex. 4: A cone-shaped vase has a height of 15 centimeters and a diameter of 8 centimeters. If one cubic centimeter is equal to one milliliter, about how many milliliters of water will the vase hold?

$$V = ? \quad h = 15 \text{ cm} \quad d = 8 \text{ cm} \quad r = 4 \text{ cm}$$

$$\begin{aligned} V &= \frac{\pi r^2 h}{3} \\ &= \frac{\pi(4)^2(15)}{3} \\ &= \frac{3.14(16)(15)}{3} \end{aligned}$$

$$V = 251.2 \text{ cm}^3$$

$$\begin{aligned} 1 \text{ cm}^3 &= 1 \text{ mL} \\ \boxed{251.2 \text{ mL}} \end{aligned}$$