# **Differentiated Instruction** for **Mathematics**

Instructions and activities for the diverse classroom

**Hope Martin** 





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# Introduction

Mathematics is the key to opportunity. . . . For students, it opens doors to careers. For citizens, it enables informed decisions. For nations, it provides knowledge to compete in a technological economy.

#### -NATIONAL RESEARCH COUNCIL (1989)

To meet the needs of all students and design programs that are responsive to the intellectual strengths and personal interests of students, we must explore alternatives to traditional mathematics instruction. We need to examine not only what is taught but how it is taught and how students learn.

Carol Ann Tomlinson in *The Differentiated Classroom: Responding to the Needs of All Learners* encourages educators to look at teaching and learning in a new way. Using the phrase "One size doesn't fit all," she presents, not a recipe for teaching, but a philosophy of educational beliefs:

- Students must be seen as individuals. While students are assigned grade levels by age, they differ in their readiness to learn, their interests, and their style of learning.
- These differences are significant enough to require teachers to make accommodations and differentiate by content, process, and student products. Curriculum tells us what to teach; differentiation gives us strategies to make teaching more successful.
- Students learn best when connections are made between the curriculum, student interests, and students' previous learning experiences.
- Students should be given the opportunity to work in flexible groups. Different lessons point toward grouping students in different ways: individually, heterogeneously, homogeneously, in a whole group, by student interests, and so forth.
- There should be on-going assessment—assessment can be used to help plan effective instruction.

To address the diverse ways that students learn and their learning styles, we can look to Howard Gardner's eight intelligences to provide a framework. Gardner's theory of multiple intelligences encourages us to scrutinize our attitudes toward mathematical learning so that each student can learn in a more relaxed environment. Let's explore what multiple intelligences look like in the mathematics classroom.



## Visual/Spatial

Perceives the visual world with accuracy; can transform and visualize three dimensions in a two-dimensional space. Encourage this intelligence by using graphs and making sketches, exploring spatial visualization problems, relating patterns in math to visual and color patterns, using mapping activities, and using manipulatives to connect concrete with abstract.



### Verbal/Linguistic

Appreciates and understands the structure, meaning, and function of language. These students can communicate effectively in both written and verbal form. Encourage this intelligence by using class to discuss mathematical ideas, using journals to explore mathematical ideas using words, making written and oral presentations, and doing research projects.



### Logical/Mathematical

Ability to recognize logical or numerical patterns and observe patterns in symbolic form. Enjoys problems requiring the use of deductive or inductive reasoning and is able to follow a chain of reasoning. Encourage this intelligence by organizing and analyzing data, designing and working with spreadsheets, working on critical-thinking and estimation problems, and helping students make predictions based upon the analysis of numerical data.



## Musical/Rhythmic

The ability to produce and/or appreciate rhythm and music. Students may enjoy listening to music, playing an instrument, writing music or lyrics, or moving to the rhythms associated with music. Activities related to this intelligence include using songs to illustrate math skills and/or concepts and connecting rational numbers to musical symbols, frequencies, and other real-world applications.



### **Bodily/Kinesthetic**

The ability to handle one's body with skill and control, such as dancers, sports stars, and craftspeople. Students who excel in this intelligence are often hands-on learners. Activities related to this intelligence include the use of manipulatives, involvement with hands-on activities (weighing, measuring, building), and permitting students to participate in activities that require movement or relate physical movements to mathematical concepts.



#### Interpersonal

The ability to pick up on the feelings of others. Students who excel in this intelligence like to communicate, empathize, and socialize. Activities related to this intelligence include using cooperative-learning groups, brainstorming ideas, employing a creative use of grouping (including heterogeneous, homogeneous, self-directed, and so forth), and using long-range group projects.



#### Intrapersonal

Understanding and being in touch with one's feelings is at the center of this intelligence. Activities related to this intelligence include encouraging students to be self-reflective and explain their reasoning, using journal questions to support metacognition, and giving students quiet time to work independently.



#### Naturalist

Naturalist intelligence deals with sensing patterns in and making connections to elements in nature. These students often like to collect, classify, or read about things from nature—rocks, fossils, butterflies, feathers, shells, and the like. Activities related to this intelligence include classifying objects based upon their commonalities, searching for patterns, and using Venn diagrams to help organize data.

# The Format of the Book

The National Council of Teachers of Mathematics (NCTM) in Principles and Standards for School Mathematics (2000) refined the 1989 standards by delineating content and process goals essential for all students, grades K-12. The chapters of this book have been organized around the content and process standards defined by the NCTM—numbers and operations, algebra, geometry and measurement, and data analysis and probability. The activities and projects in each chapter reflect the philosophy of differentiation, provide a math curriculum that is standards-based, and involve students in hands-on, motivating real-world problems. Each chapter ends with a "Brush Up Those Skills" game that supports flexible grouping and employs the skills and concepts introduced in the chapter's activities. The Appendix contains copies of a blank Teacher's Page, Task/ Audience/Product (TAP) Activities page, and "Brush Up Those Skills" pages to help the teacher design and organize his or her own differentiated mathematics lessons. One of the lessons, "How Long Is Your First Name?" requires students to use one-inch squares, and a "Brush Up Those Skills" activity requires a copy of Pascal's triangle-so these sheets have been provided, as well. The Teacher's Pages require additional discussion.

# **Using the Teacher's Pages**

Each mathematical experience is preceded by a Teacher's Page that includes valuable information for managing the lesson. These pages have been designed to merge the NCTM's mathematics standards and the philosophy of differentiation.

- Math Topics: As in most hands-on activities, these mathematical experiences address more than one math skill or topic. In the real world, mathematics is an integrated experience, and skills and concepts interrelate and blend. When using the activities, teachers can use this section to connect the lesson to skills and concepts that are part of their mathematics curriculum.
- **Prior Knowledge Needed:** Differentiating necessitates that the teacher know their students' prior knowledge. This information can be gained in a variety of ways—through pretesting, observation and questioning, or available data from other sources. To be assured that each student's experience is meaningful and enriching, it is important to know where to start.

### • Differentiation Strategies

**Principles:** The three principles of differentiation are respectful tasks, flexible grouping, and ongoing assessment. Applicable principles are discussed in this section.

**Teacher's Strategies:** Teachers can differentiate content, process, and/or product. Every student should be exposed to a mathematics curriculum that is equitable, essential, and requires higher-level thinking skills. Those differentiation strategies that can be used to accommodate diverse learners can be found in this section.

According to Students: Students' readiness, interests, and learning styles determine the accommodations made in a differentiated classroom. Pretest and interest surveys can be taken at any time to meet student needs. This section suggests the multiple intelligences and learning styles that are highlighted in the activity.

### Materials Needed

A comprehensive list of materials and supplies needed for each activity is provided. To help the activity run more smoothly, these should be gathered and made ready prior to the lesson.

### • Teaching Suggestions

**Engaging the Students:** Suggestions are made to begin the lesson and perk student interest. There may be a song or a poem that will draw student attention. This engaging activity varies with the lesson. Productive questioning is sometimes suggested to focus students on the lesson. Productive questioning include these questions:

- Focus attention (What have you noticed about . . . ? What do you see when you . . . ?)
- Help students count or measure (How many . . . ? How long . . . ? How much . . . ?)
- Comparison questions (What do these have in common with . . . ? How are they different?)

- Problem-posing questions (What problems did you face when . . . ? How did you solve this problem?)
- Reasoning questions (Why do you think . . . ? What is your reason for . . . ? Can you come up with a rule for . . . ?)

These types of questions can also be used during debriefing or as ongoing assessment during observation of students.

The Exploration: "Engaging the Students" usually has students discussing and working as a whole group. If students are going to work individually, with a partner or in a group of four, the regrouping will be done at this time. While this section is not a scripted, step-by-step plan, it does give suggestions to help teachers encourage students and make the experience more meaningful. Some lessons do suggest specific questions that will help students focus or develop understanding. But these are merely suggestions and should be used only if appropriate to the needs of the class. Available answers also appear in this section.

**Debriefing:** During this time groups, will come back together to discuss their findings and share their results. Many of the activities ask students to share their data on a group data table for further analysis. Productive questions can be used at this time to help focus students' attention on the important concepts and skills presented in the activity.

### Assessment

Multiple suggestions are made here. They may include the following: (1) completed student products, (2) observation and questioning, (3) tiered or non-tiered journal question(s), and (4) TAP activities.

Many types of activities can be tiered, such as assignments, journal questions, warmups, and activities. A few suggestions to help plan tiered activities are as follows:

- 1. All levels should apply the same skill or concept.
- 2. All levels should meet student readiness.
- 3. All levels should challenge students and provide new learning experiences.
- 4. Higher difficulty levels should be a more faceted problem, have less structure, and require more independence of the students.
- 5. All levels should build on student knowledge and require higher level thinking skills.

Task/Audience/Product (TAP) activities are adapted from Tomlinson's RAFT activities. They are used sparingly in assessment suggestions, but a blank form is located in the Appendix section of this book. This form can be used to develop your own assessment activities.

• Variations for Differentiation (Tiered Activities): Some of the activities can be tiered or elaborated upon, and suggestions have been made in this section. If the teacher has any activities that can be added to enhance the lesson, this would be a fine place in which to list those for future use.

# Number Theory, Numeration, and Computation

There is nothing so troublesome to mathematical practice . . . than multiplications, divisions, square and cubical extractions of great numbers . . . I began therefore to consider . . . how I might remove those hindrances.

#### -JOHN NAPIER

Number theory, numeration, and computation remain important components of the current school mathematics curriculum. While it is true that computation and basic number facts have been emphasized to the detriment of other strands of mathematics, we all understand that student proficiency in these areas is essential for students to be successful in understanding math concepts. With guidance and meaningful experiences, students will gain a sense of number, improve their ability to solve problems, and develop useful strategies to estimate reasonableness of answers. The activities and projects in this chapter will encourage the development of number and operation sense in students.

"The Bowling Game" (page 3) gives students the opportunity to practice order of operations and computational skills in an interesting way. The numbers used in the game are determined by chance according to the roll of one die. Individual creativity and imagination are rewarded in points gained. The lesson can be augmented by using a little ditty, " $O^3$ —Order of Operations Song" (page 6). This makes learning the rules even more fun and draws attention to the musical/rhythmic intelligence!

"All About the Moon" (page 8) demonstrates the connections between math and science while presenting computation, estimation, conversions, and open-ended problem solving as captivating activities. Interesting moon facts are explained in a way that makes sense to students, and very large numbers become more understandable through hands-on activities. By encouraging students to work collaboratively, a variety of differentiation strategies can be utilized.

When patterns found in numbers are translated into fascinating visual patterns, students can investigate the relationship between art and mathematics; skills and concepts are learned using a variety of learning styles and intelligences. In "The Pattern Tells It All" (page 12), students learn how prime and composite numbers form patterns in number grids that are visually different. By writing about their patterns, students verbalize the depth of their understanding.

When students can see connections between school math and real math, they are motivated to learn important concepts and skills. "Baking Blueberry Muffins" (page 18) shows students mathematics applications that utilize ratio and proportion, percent of profit, and everyday conversions. While students work together on this activity, they make use of many of the strategies of differentiated instruction.

By using the rules of divisibility and some simple computation, students can discover all of the prime numbers less than 500 using "Eratosthenes and the 500 Chart" (page 21). "The Divisibility Ditty" (page 115) reminds students of the divisibility rules while encouraging students to use a variety of intelligences to learn important mathematics concepts.

Finally, "Diagramming Divisibility" introduces Venn diagrams—using logic to reinforce divisibility rules in yet another way. "The Divisibility Ditty" can be used again to review these important rules.

# Patterns, Functions, and Algebra

In mathematics he was greater Than Tycho Brahe, or Erra Pater: For he, by geometric scale, Could take the size of pots of ale; Resolve, by sines and tangents straight, If bread or butter wanted weight And wisely tell what hour o' th' day The clock does strike by algebra.

#### -SAMUEL BUTLER (1612-1680)

When students study algebra the most common question usually is, "When are we ever going to have to use this?" Rather than present algebra as a set of rules and procedures, the lessons in this chapter relate algebra to real-world phenomena and motivating activities.

We start off with a contest—which pair of students can land their parachutes the closest to each other? In the "The Parachute Jump," students work in pairs to design parachutes and use the Pythagorean theorem to calculate the distance between their "jumps." Using the song "Ode to Pythagoras" (page 37) and their active involvement, students begin to see the real-world applications of algebra while using a variety of learning styles to better understanding this concept.

The Pythagorean theorem is revisited in "The Irrational Spiral" (page 43), but this time students experiment with algebra, geometry, and design. The lesson begins by "replaying" the musical ditty "Ode to Pythagoras." Students, using protractors and rulers, draw a right triangle with a base and height of 1 cm and progress to design an amazing spiral design.

The activity "Seeing to the Horizon" (page 44) explains the scientific principle that on a clear day, "the higher up you are, the further you can see." A list of the ten tallest skyscrapers is provided and, using an algebra formula, students calculate how far they can see from the rooftops of these buildings. This is the perfect time to work with the art teacher and introduce perspective and vanishing points to students. Students continue to research the height of their school building, but this time using stopwatches and marshmallows. In "Falling Objects: Formulas in the Real World" (page 49), students start out with skyscrapers and then use marshmallows, stopwatches, and algebraic formulas to estimate the height of their school in a unique way.

And finally, "Pattern Block Patterns" (page 55) uses hands-on manipulatives to have students build geometric patterns. By describing, analyzing, and replicating the pattern, they are using algebraic reasoning while utilizing different learning styles and intelligences.

Cokie Roberts is quoted as saying, "As long as algebra is taught in school, there will be prayer in school." Perhaps if students are given the opportunity to experience hands-on activities related to algebra, the subject will not generate such aversion and apprehension.

# **The Parachute Jump**

# MATH TOPICS

ordered pairs on the coordinate plane, the Pythagorean theorem, data collection and analysis

# PRIOR KNOWLEDGE NEEDED

- 1. understanding of (x, y) coordinates on the coordinate plane
- 2. knowledge of the Pythagorean theorem

## DIFFERENTIATION STRATEGIES

### Principles

Flexible grouping: For this activity, students work in pairs. While this activity is designed to help students calculate the distance between two points on the coordinate plane using the Pythagorean theorem, the activity can be tiered. More advanced students can be taught the distance formula and use the formula to find the distance.  $D = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$ .

Ongoing assessment: Observe students during the activity, and use data collection sheets to assess level of understanding.

## **Teacher's Strategies**

Product: Tiered Journal Questions: The Level 1 question is an easier question because it asks students to explain, in their own words, what happened in the experiment that uses the Pythagorean theorem. The Level 2 question is written for students who used the distance formula. It asks them to explain why the distance formula is a shortened version of the Pythagorean theorem.

## According to Students

Learning Styles/Multiple Intelligences: logical/mathematical, bodily/kinesthetic, musical/rhythmic, visual/spatial, verbal/linguistic, interpersonal

# MATERIALS NEEDED

Each pair of students will need the following:

1. two coffee filters

Visual O space

- 2. eight 12-inch lengths of thread
- 3. a paper punch
- 4. large safety pins, large paper clips, or washers
- 5. colored pencils or markers
- 6. poster board or a large sheet of graph paper
- 7. a student activity sheet
- 8. data collection table

### **TEACHING SUGGESTIONS**

### **Engaging the Students**

Discuss with students the parachute jump experiment. Have two parachutes made to represent the two students' parachutes. Drop one previously made parachute onto a coordinate plane and mark that point. Now drop the second one; mark that point as well. Lightly draw a line connecting the two drop points. Discuss with students that the length and width of each of the squares on the graph represent a side of 1 and ask, "Can the distance between the two drop points be measured as if it were the side of a square?" Using a pencil, lightly draw a vertical line from one drop point and a vertical line from the other drop point. These two lines will form the legs of a right triangle—the line connecting the distance between the two drop points is the hypotenuse of this triangle. Discuss with students how the Pythagorean theorem can be used to approximate the length of the distance between the drop points.

### The Exploration

The song "Ode to Pythagoras" can be sung before this experiment is conducted. This is an interesting way to review the Pythagorean theorem and is most effective with students with a variety of learning styles.

Students are placed into pairs and given one student activity sheet. This sheet contains a set of directions to help them design and build their own parachute to use in the experiment and fill out the data collection table. Four holes are evenly spaced around the edge of a coffee filter, and string (about 12 inches long) is attached to each hole. A large paper clip or washer must be attached to the string to help the parachute land. Students may decorate their parachutes for purposes of identification.

Each team must divide a poster board into 4 quadrants, labeling the x and y coordinate points unless large sheets of graph paper are available for their use. (An overhead transparency can serve as a sample for the groups.)

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Each team member, taking turns, drops his or her parachute onto the poster board. Each landing location (the x and y coordinate point) is recorded in the data collection table.

It is possible to form a right triangle by connecting the two landing points (this line becomes the hypotenuse of the right triangle) and then drawing the horizontal and vertical lines from these points to form the legs of the triangle. The lengths of the vertical line (side *b*) and horizontal line (side *a*) can be easily calculated and the Pythagorean theorem  $(a^2 + b^2 = c^2)$  can be used to find the distance between the two landing points. For example, if the two parachutes land on the coordinates indicated on this graph, the length of side a = 2 and the length of side b = 3;  $2^2 + 3^2 = c^2$ .  $4 + 9 = c^2$ ;  $c = \sqrt{13} \approx 3.6$ . For those students using the distance formula, this formula can be easily substituted in the data collection table in the last column. Students will conduct ten drops and find the average or mean distance between them.



### Debriefing

Give each group time to discuss their results and the mean distance between the ten drops. You can award a prize to the team with the shortest mean distance.

#### ASSESSMENT

- 1. Student products: Make sure students have successfully completed activity sheets.
- 2. Journal questions:
  - a. Level 1 question: Discuss the interesting aspects of your experiment by describing 1) how you used the Pythagorean theorem to help you find the distances, 2) why you could not just measure the distance between the two coordinate points, 3) your results (if landings in one quadrant occurred more often than another, if the parachute drifted or always landed in the same location, and why you think this occurred).
  - b. Level 2 question: Analyze both the Pythagorean theorem and the distance formula. Explain why the distance formula is actually the Pythagorean theorem expressed in another way and why either one can be used to find the hypotenuse of a right triangle.

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# **Ode to Pythagoras**

#### SUNG TO "HOKEY POKEY"

You take your first leg "*a*," And then your next leg "*b*," Take the sum of their squares, Are you following me?

To use this famous theorem, For Pythagoras let's shout, That's what it's all about.

We're not quite finished yet, Cause there's a third side to see, You know this tri-angles right, Are you following me?

To use this famous theorem, For Pythagoras let's shout, That's what it's all about.

Now add the square of leg "*a*," To the square of leg "*b*," You get the square of side "*c*," Are you following me?

To use this famous theorem, For Pythagoras let's shout, That's what it's all about.

 $a^2 + b^2 = c^2$ 

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# **The Parachute Jump**

Directions: Work with a partner to complete the following activity.

- A. You will need:
  - 1. one coffee filter
  - 2. four pieces of string  $\approx 12$  inches long
  - 3. a large paper clip, large safety pin, or washer
  - 4. one piece of poster board or large sheet of graph paper for you and your partner
  - 5. one data collection table for you and your partner
  - 6. colored markers or colored pencils
- B. You will need to create and design your own parachute. Punch four holes near the edge of a coffee filter at evenly spaced intervals. Attach four pieces of string (12 inches long) in each of the holes. Draw the four pieces of string together and attach a large paper clip, a safety pin, or a washer at the end of the connected string. Be sure to decorate your parachute for ease in identification.
- C. Work with your partner to create a "landing area" for the parachutes.
  - 1. Divide the poster board or your large sheet of graph paper into 4 quadrants.
  - 2. Label the x and y coordinate points.
- D. Drop your parachutes (one at a time) from the designated height above the landing area. The "landing location" is the nearest (x, y) point on the "landing area." Record ten successive drops for you and your partner on the data collection table.
- E. Use graph paper after each "drop" to plot the coordinate points for your drop and your partner's drop. Connect the two points, and draw a horizontal line from one of the points and a vertical line from the other. You have now formed a right triangle. Use the Pythagorean theorem to find the length of the hypotenuse of this triangle.
- F. After your ten trials, find the mean difference of distance between the parachute drops. Compare your results with other groups. How did your distances compare?

# **The Parachute Jump**

DATA COLLECTION

Trial Number	(x, y) Coordinates of Team Member 1	(x, y) Coordinates of Team Member 2	Length of Side <i>a</i>	Length of Side <i>b</i>	Distance Between Landing Locations of Parachutes 1 and 2: $a^2 + b^2 = c^2$
1					
2					
3					
4					
5					
6					
7					
8					
9					
10					
Mean					

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# **Selected Answers**

#### Page 11-All About the Moon

- 1. The crater is just slightly smaller than the size of South Carolina (31,000-sq. mi.) but more than three times the size of the state of New Jersey (7,787 sq. mi.).
- 2. It would take 8 years, 267 days for the train to reach the moon.
- 3. The moon rock costs \$30,000,000/lb. or \$1,875,000/oz.

### Page 20—Baking Blueberry Muffins

- A. 1. 96 muffins
  - 2. 0.375 each or  $37\frac{1}{2}$ ¢ each
  - 3. 300% profit
- B. 1. 57 muffins (there is a remainder but that is not enough to make another muffin)
  - 2. \$0.64 each (although the remainder is less than  $\frac{1}{2}$ , it is added on to calculate cost)
  - 3. \$30.72/dozen (students may round up the number to a more reasonable amount)

#### Page 29–Diagramming Divisibility

The answers are located on page 27 of the teacher's page.

#### Page 47–Seeing to the Horizon

The answers are located on page 45 of the teacher's page.

### Page 53-Falling Objects: Formulas in the Real World

The answers are located on page 51 of the teacher's page.

### Page 57—Pattern Block Patterns

The fifth term will have 4 triangles and 5 trapezoids.

Since each term has t-1 # of triangles and t # of trapezoids, the 20th term will have 19 triangles and 20 trapezoids; the hundredth term will have 99 triangles and 100 trapezoids; the *n*th term will have n-1 triangles and *n* trapezoids.

#### Page 65–Pennies and the Sears Tower

The number of pennies needed to reach a height of 1450 feet will depend on the studentexplorations. The students' calculations will depend on the age of their pennies, the number of pennies they used to make their estimates, and the accuracy of their measurements. Because of all of these variables, it is necessary to collect the data from all of the groups and analyze the individual results.

#### Page 106–Vowels, Vowels, Everywhere

The vowel A appears in the poem 41 times or 6.4% of the total # of letters (639). The vowel E appears in the poem 95 times or 14.9% of the total # of letters (639). The vowel I appears in the poem 55 times or 8.6% of the total # of letters (639). The vowel O appears in the poem 43 times or 6.7% of the total # of letters (639). The vowel U appears in the poem 16 times or 2.5% of the total # of letters (639).

Page 106–Vowels	, Vowels,	Everywhere
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Vowels	Frequency	Fraction	Percentage	# of ° in circle
А	41	41/250	16.4%	59°
Е	95	95/250	38.0%	137°
Ι	55	55/250	22.0%	79°
О	43	43/250	17.2%	62°
U	16	16/250	6.4%	23°
TOTAL	250	250/250 = 1	100.0%	360°

#### Page 120-121-Geometric Probability: Dartboards and Spinners

Answers are on page 118 of the teacher's page.

Based on the theoretical probabilities of each of the colors, the sections of the circle graph should be Red- $60^{\circ}$ , Yellow- $120^{\circ}$ , Green- $100^{\circ}$ , and Blue- $80^{\circ}$ .

#### Page 128—Flipping Three Coins: Heads or Tails

The theoretical probability of each occurrence is found on page 126 of the teacher's page.